

## **Effect of the Sleeve Profile on the Stability of Rotor Operating in Multilobe Journal Bearings**

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### **Abstract**

Multilobe journal bearings with the sleeve of the 2-, 3 or 4- sliding lobes of cylindrical profile are applied in different types of rotating machinery. The design of such journal bearings, the number of lobes and oil grooves improves thermal state of bearing at higher speeds and the stability of operation.

The paper describes the results of the calculations of dynamic characteristics and determination of stability ranges of simple symmetric rotor operating in the offset types of multilobe journal bearings. The dynamic characteristics of supporting bearings are defined by four stiffness and damping coefficients of oil film. The iterative solution of Reynolds, energy and viscosity equations allows the obtaining of the load capacity of bearings and the required dynamic coefficients of oil film. Adiabatic, laminar oil film and the static equilibrium position of journal were assumed. The oil film pressure, temperature, viscosity fields and the oil film forces were the basis of the bearing dynamic characteristics and stability determination.

**Keywords:** multilobe, offset journal bearings, stability of rotor

### **1. Introduction**

The stability of rotor operating in journal bearings can be determined on the basis of supporting bearings dynamic characteristics expressed by the stiffness and damping coefficients of oil film [1-6]. The multilobe bearings, mostly used in slightly loaded, high speed rotating machines are characterised by good damping of vibrations and good stability of operation [1-3]. Exemplary types of such bearings are the 2- (offset-halves) [6], 3-and 4-lobe offset bearings [7-11] that are applied in the turbine gearboxes [6].

The design of 2-, 3- or 4-lobe journal bearings, the number of lobes and oil grooves improves the thermal state of bearing and stability of operation [1-3]. These multilobe journal bearings can be manufactured as the bearings with cylindrical sliding surfaces [5], with pericycloid profile of bearing bore [7,8] or as the offset ones [6,9].

Typical multilobe (classic) journal bearing is composed of single circular sections whose centres of curvature are not in the geometric centre of the bearing. The geometric configuration of the bearing as a whole is discontinuous and not circular. The multilobe pericycloid journal bearings ("wave bearings" [7,8]) is characterised by continuous profile and multihydrodynamic oil films on the journal perimeter.

The characteristic feature of multilobe, offset journal bearings are that the circle inscribed in the bearing profile touches the end of the convex gap of the bearing [5,6] in the direction of journal rotation (Fig. 1).

The paper presents the effect of sleeve profile on the stability of simple symmetric, elastic rotor operating in 2-, 3- and 4-lobe offset journal bearings. The oil film pressure,

temperature and viscosity fields that are required for the calculations of the bearing static and dynamic characteristics, have been obtained by iterative solution of the Reynolds', energy and viscosity equations. Adiabatic, laminar oil film and the static equilibrium position of journal were assumed. The dynamic characteristics of journal bearing are the basis of stability ranges determination [1-3]. All the stiffness and damping coefficients were calculated by means of perturbation method [1,6].

## 2. Stability of elastic rotor

Considered multilobe, offset type journal bearings are presented in Fig. 1. Their geometry can be found in [5,6].

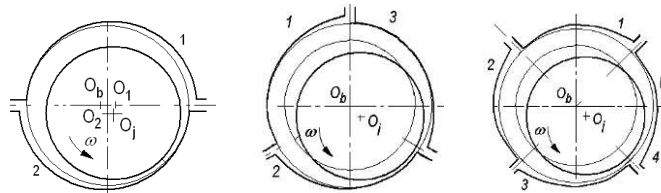


Figure 1. Lay-out of the 2-, 3-, and 4-lobe offset journal bearings;  $O_b$ ,  $O_j$ ,  $O_1$ ,  $O_2$  – centres of bearing, journal, upper and bottom lobe (2-lobe offset bearing),  $1 \div 4$  number of lobes

The journal bearing static and dynamic characteristics for adiabatic or diathermal model of oil film can be determined by the numerical solution of the oil film geometry, Reynolds, energy, viscosity [2,6] equations. The stiffness  $g_{ik}$  and damping  $b_{ik}$  coefficients allow the determination of stability ranges [1-8].

The equations of motion for the journal and the centre of elastic shaft are given in matrix form by Eqn. (1) [4].

$$M \cdot \ddot{x} + B \cdot \dot{x} + C \cdot x = \hat{a} \cos \omega t + \hat{b} \sin \omega t \quad (1)$$

where:  $M$ ,  $B$ ,  $C$  – matrices of mass, damping and stiffness,  $\hat{a}$ ,  $\hat{b}$  – coefficients of dynamic constraints,  $\omega$  – angular velocity, ( $s^{-1}$ ).

After transformations of Eqn. (1) the real and imaginary part was obtained [1,4]. The stability of elastic rotor-bearing system is analysed based on the following characteristic frequency equation of 6-th order with regard to  $(\lambda/\omega)$  [1-6].

$$c_6 \lambda^6 + c_5 \lambda^5 + c_4 \lambda^4 + c_3 \lambda^3 + c_2 \lambda^2 + c_1 \lambda + c_0 = 0 \quad (2)$$

1.

2. Solution assumption for Eqn. (2) is  $\lambda_j = -u_j + iv_j$  ( $1 \leq j \leq 6$ ), with  $u$  as damping and  $v$  representing the self-vibrations. Stability of the linear vibrations of system occurs only when all real parts of eigenvalues  $\lambda_j$  are negative. The coefficients  $c_0$  through  $c_6$  in Eqn. (2) are the functions of  $a_0$ ,  $b_0$ ,  $g_{ik}$ ,  $b_{ik}$ .

$$c_0 \div c_6 = f(a_0, b_0, g_{ik}, b_{ik}) \quad (3)$$

where:  $a_0$  - ratio of angular velocity  $\omega$  to the angular self-frequency of stiff shaft,  $a_0 = (\omega / \omega_c)^2$ ,  $\omega_c$  - angular self frequency of stiff rotor,  $\omega_c = \sqrt{c^* / m}$ ,  $b_0$  - ratio of Sommerfeld number to the relative elasticity of shaft,  $b_0 = So / c_s$ ,  $c^*$  - shaft stiffness, (N  $m^{-1}$ ),  $c_s$  - relative elasticity of shaft,  $c_s = f / \Delta R = g / (\omega_c^2 \cdot \Delta R)$ ,  $f$  - static deflection of shaft, (m),  $F$  - resultant force of oil film (N),  $F_{stat}$  - static load of bearing, (N),  $g$  - acceleration of gravity, (m  $s^{-2}$ ),  $g_{ik}$  - dimensionless stiffness coefficients,  $g_{ik} = So(\Delta R / F_{stat})$ ,  $g'_{ik}$  - stiffness coefficients, (N/m),  $b_{ik}$  - dimensionless damping coefficients,  $b_{ik} = So(\Delta R / F_{stat}) \omega \cdot b'_{ik}$ ,  $b'_{ik}$  - damping coefficients, (N s / m),  $m$  - mass of the rotor, (kg),  $So$  - Sommerfeld number,  $So = F \cdot \psi^2 / (L \cdot D \cdot \eta \cdot \omega)$ ,  $So_k$  - critical Sommerfeld number,  $So_k = So \omega / \omega_c$

Coefficients of characteristic Eqn. (2) depend on the stiffness and damping coefficients, Sommerfeld number  $So$ , relative elasticity of shaft  $c_s$  and the ratio of angular velocity to the critical angular velocity of stiff rotor. The expression determining the ratio of boundary angular speed  $\Omega_b$  to the critical  $\omega_c$  one, and the stability of rotor [1-4], is:

$$\left( \frac{\Omega_b}{\omega_c} \right)^2 = \frac{1}{1 + b_0 \cdot \frac{A_3}{A_1}} \frac{A_2 \cdot A_3^2}{A_1^2 + A_1 \cdot A_3 \cdot A_4 + A_0 \cdot A_3^2} \quad (4)$$

where:  $A_0, A_1, A_2, A_3, A_4$ , consist the stiffness  $g_{ik}$  ( $i=1,2$  and  $k=1,2$ ) and damping  $b_{ik}$  ( $i=1,2$  and  $k=1,2$ ) coefficients [1-6],  $\Omega_b$  - boundary angular velocity ( $s^{-1}$ )

### 3. Results of calculations

The stability of simple elastic, symmetric rotor (Jeffcott rotor) was determined with the use of the calculated dynamic characteristics. The calculations included the non-dimensional load capacity  $S_0$  and journal displacement  $\varepsilon$  as well as the static equilibrium position angles  $\alpha_{eq}$ , too. The offset journal bearings under consideration have the length to diameter ratio  $L/D=0.6$ ,  $L/D=0.75$  and  $L/D=0.8$ . Different lobe relative clearances  $\psi_s$  (for the 3-lobe pericycloid bearing its relative eccentricity was  $\lambda^* = 0.25$  [6,7]) and rotational speeds were assumed. The bearing relative clearances were  $\psi = 0.9\%$ ,  $\psi = 1.5\%$  and  $\psi = 2.7\%$ . The feeding oil temperature was  $T_0=40^\circ C$  and the corresponding thermal coefficients  $K_T$  [2,8] were 0.139, 0.215 and 0.315;  $K_T = \omega \cdot \eta_0 / (c_t \cdot \rho \cdot g \cdot T_0 \cdot \psi^2)$  where:  $c_t$  - specific heat of oil, (J/kgK),  $g$  - acceleration of gravity (m/s<sup>2</sup>),  $\eta_0$  - dynamic viscosity of supplied oil (Ns/m<sup>2</sup>),  $\rho$  - oil density, (kg/m<sup>3</sup>),  $\psi$  - bearing relative clearance, (%).

Exemplary results of the calculations of dynamic characteristics and stability are shown in Fig. 2 through Fig. 15. The stiffness  $g_{ik}$  and damping  $b_{ik}$  coefficients are given in Fig. 2 through Fig. 7. The stability ranges can be observed in Fig. 8 through Fig. 15.

Fig. 2 and Fig. 3 show the stiffness and damping coefficients of the offset-halves bearing with the lobe relative clearance  $\psi_s=2$ . The largest values have the coefficient  $g_{22}$  for the Sommerfeld numbers over 0.44. The values of the coupled damping coefficients  $b_{12}$  and  $b_{21}$  are very close (e.g. Fig. 3). The damping coefficient  $b_{11}$  is larger than the ones  $b_{12}$  and  $b_{21}$  in the range of Sommerfeld numbers  $S_0$  from 0 to about 0.6. At increasing values of Sommerfeld numbers, the coefficient  $b_{11}$  is smaller than the coupled terms  $b_{12}$  and  $b_{21}$  (Fig. 3).

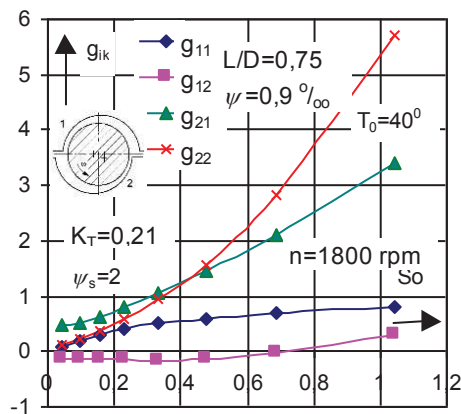


Figure 2. Stiffness coefficients of offset-halves offset-journal bearing

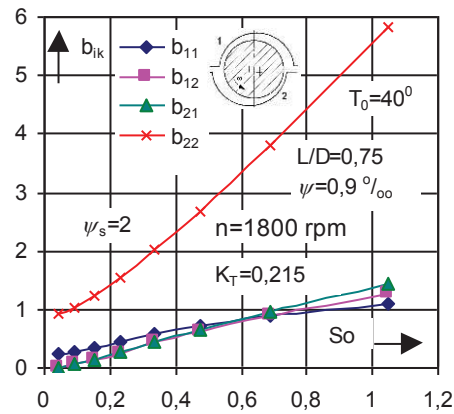


Figure 3. Damping coefficients of halves journal bearing

The stiffness and damping coefficients of the 3-lobe offset journal bearing are presented in Fig. 4 and Fig. 5. The bearing length to diameter ratio  $L/D=0.8$ , clearance ratio  $\psi=1.5\text{‰}$  and lobe relative clearance  $\psi_s=2$  were assumed. Heat number  $K_T$  was  $K_T=0.315$ . The largest values have the coefficients  $g_{22}$  and  $b_{22}$  but the smallest  $g_{12}$  and  $b_{21}$  (Fig. 4 and Fig. 5). The values of the coupled damping coefficients  $b_{12}$  and  $b_{21}$  are very close and  $b_{11}$  is larger than the coupled coefficients (Fig. 5).

The stiffness and damping coefficients of 4-lobe offset bearing are given in Fig. 6 and Fig. 7. The largest values has the stiffness coefficient  $g_{21}$  and the smallest value the coefficient  $g_{11}$  (Fig. 6); In the range of Sommerfeld number from nil to about 0.12 the coefficient  $g_{22}$  is larger than  $g_{12}$  but at higher Sommerfeld numbers there is reverse dependence. The damping coefficient  $b_{22}$  is the largest and the coupled coefficients have the smallest, equal values, i.e.  $b_{12}=b_{21}$  (Fig. 7).

The stability ranges of symmetric rotor operating in 2-lobe offset bearings with the lobe relative clearance  $\psi_s=1$  (Fig. 8 - cylindrical sliding surfaces) and  $\psi_s=2$  (Fig. 9 - lemon shaped sliding surfaces) show the difference. The rotor running in the bearings characterized by the value of lobe relative clearance  $\psi_s=2$  shows larger range of stability (e.g. Fig. 8 and Fig. 9).

Exemplary results of stability ranges that were obtained for 3-lobe offset journal bearing at different values of lobe relative clearance  $\psi_s$  and at different relative elasticity of shaft

$c_s$  are shown in Fig. 10 and Fig. 11. At the values of the relative elasticity of shaft under consideration there is an increase in the stability at the increase in the lobe relative clearance  $\psi_s$  (e.g. the curves for  $c_s=0.1$  in Fig. 10 and Fig. 11). The coefficient  $\text{tg } \tau$  in the range of larger critical Sommerfeld numbers  $S_{ok}$  is the measure of stability properties of bearing [2,3]. Larger values of angle  $\tau$  mean the larger range of stability, i.e. at assumed load of bearing there is higher boundary of stability  $\Omega_b/\omega_c$  [2,3].

For the comparison task, the stability ranges of rotor operating in 3-lobe pericycloid journal bearing and in classic 3-lobe bearing are shown in Fig.12 and Fig. 13. It results from the comparison that the 3-lobe offset bearing has better stability properties than the 3-lobe pericycloid and 3-lobe classic bearings.

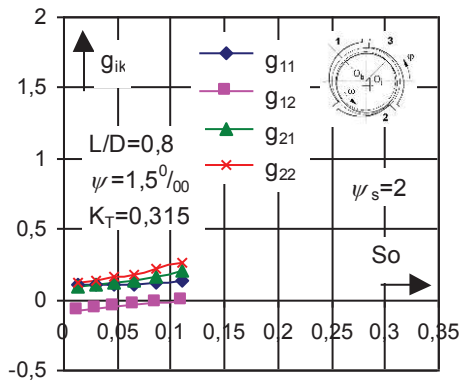


Figure 4. Stiffness coefficients of 3-lobe offset journal bearing

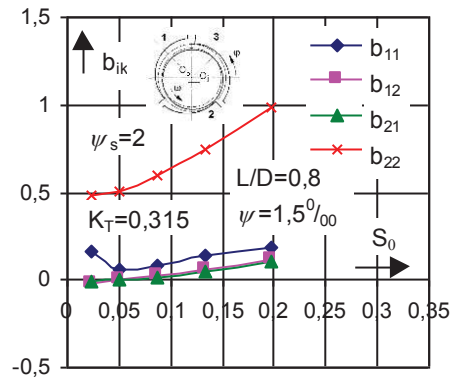


Figure 5. Damping coefficients of 3-lobe offset journal bearing

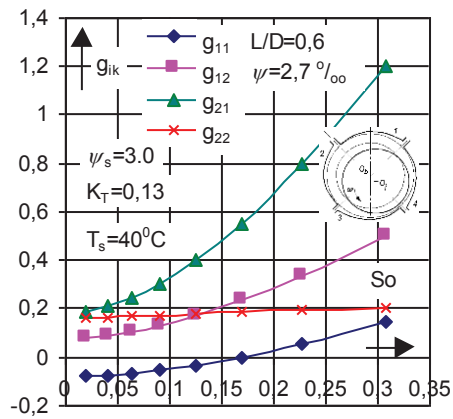


Figure 6. Stiffness coefficients of 4-lobe offset journal bearing

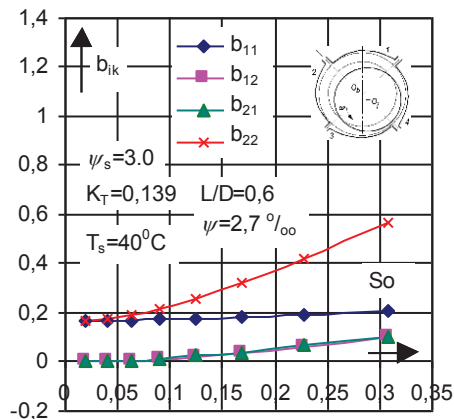


Figure 7. Damping coefficients of 4-lobe offset journal bearing

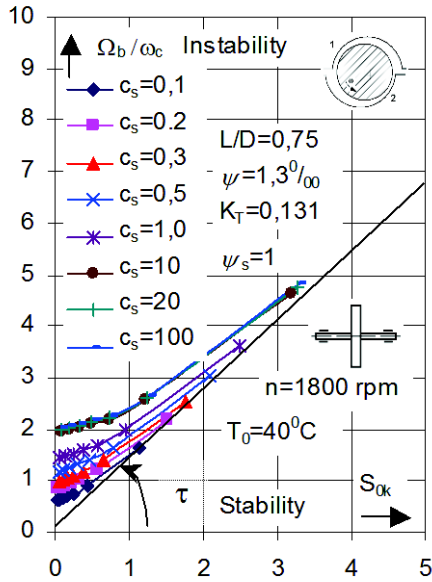


Figure 8. Stability chart of rotor operating offset-halves journal bearings ( $\psi_s = 1$ )

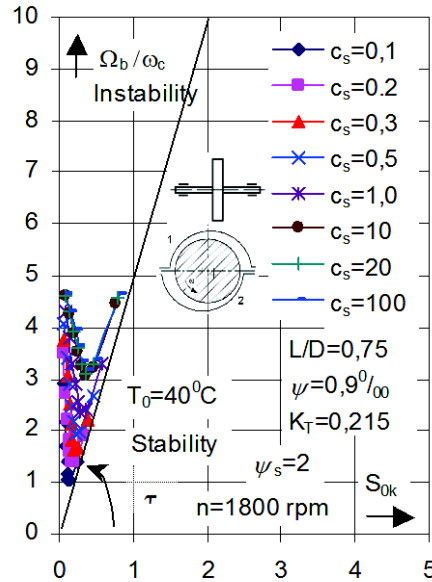


Figure 9. Stability chart of rotor operating in offset-halves journal bearings ( $\psi_s = 2$ )

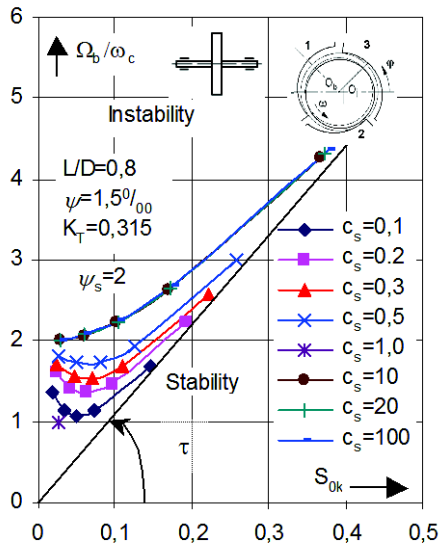


Figure 10. Stability chart of rotor operating 3-lobe offset journal bearing

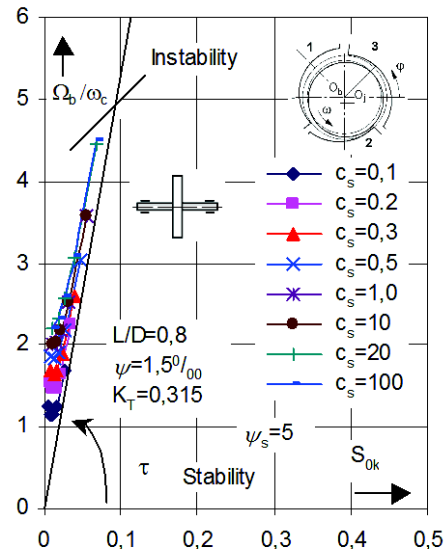


Figure 11. Stability chart of rotor operating in 3-lobe offset journal bearing

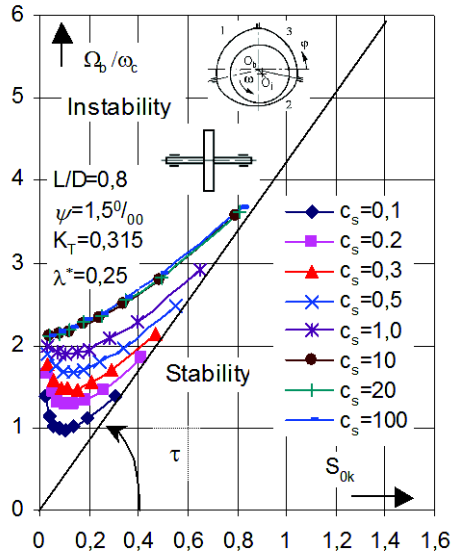


Figure 12. Stability chart of rotor operating in 3-lobe pericycloid journal bearing

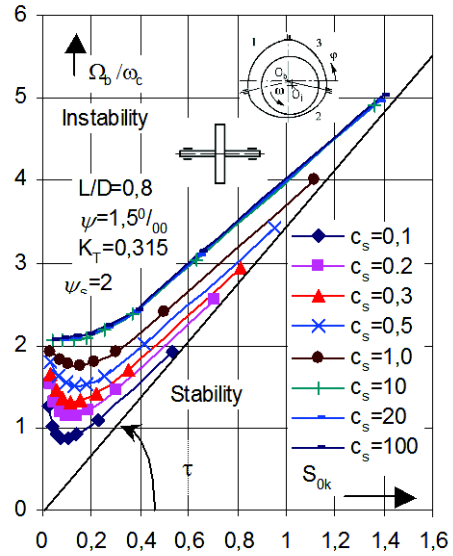


Figure 13. Stability chart of rotor operating in 3-lobe journal bearing

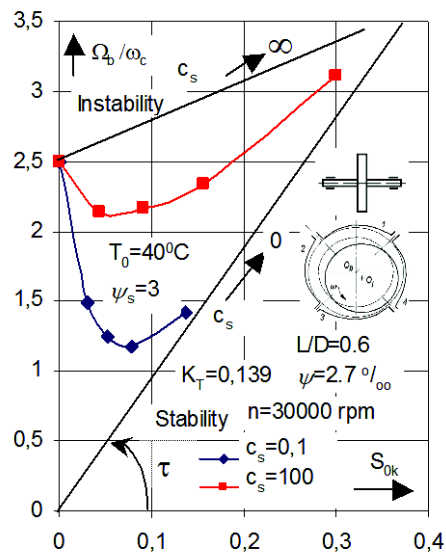


Figure 14. Stability of elastic rotor operating in 4-lobe offset journal bearing at the lobe relative clearance  $\psi_s=3$

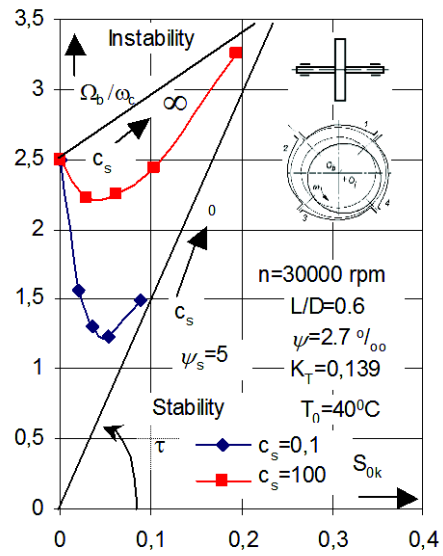


Figure 15. Stability of elastic rotor operating in 4-lobe offset journal bearing at the lobe relative clearance  $\psi_s=5$

#### 4. Conclusions

Dynamic characteristics including the stability ranges of the chosen types of offset bearing with different sleeve profiles and on the assumption of adiabatic model of oil film, were obtained by means of perturbation method. Investigation that were carried out at assumed geometric and operating parameters, various relative shaft elasticity values, allows to draw the following conclusions:

1. Static and dynamic characteristics of the considered journal bearings of different sleeves profiles can be obtained from developed program of numerical calculations.
2. The offset type multilobe journal bearings show better stability than the classic multilobe bearings.
3. An increase in the relative elasticity of shaft increases the range of rotor stability.
4. The results of developed program form the input data for the investigation and analysis into the stability of different types of multilobe journal bearings.

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